The pattern and magnitude of rotational piezomagnetic anomalies along the dip-slip Mosha fault, Northern Tehran, Iran

M. Mokhtari\textsuperscript{1} and S. Kiarasi\textsuperscript{2}

\textsuperscript{1}International Institute of Earthquake Engineering and Seismology, No.26, Dibajie Shomali, Tehran, Iran
\textsuperscript{2}Azad University, Ponk, Tehran, Iran

Received: 21 July 2008 – Revised: 7 October 2008 – Accepted: 8 October 2008 – Published: 28 November 2008

Abstract. Several active faults affect the Central Alborz, Northern Iran. The main active faults in the region are the North Tehran and the Mosha faults and their westward continuation, the Taleghan fault. Among these the Mosha fault is the most active fault in Central Alborz. The piezomagnetic field has been inspired by many investigations in the earthquake prediction studies and has been reported in the literature. Several theories proposed for relating piezomagnetic changes into magnetic signals accompanying earthquakes in the vicinity of a fault. In this study based on an analytical solution for the elementary piezomagnetic potentials due to an inclined rectangular fault within a semi-infinite elastic medium a computer program has been developed. This program has been used for evaluation of the rotational piezomagnetic changes along the Mosha fault using different earthquakes with specific magnitudes and at the presence of three different geomagnetic main fields. The magnetic data acquired recently at the study area has been used during the modeling. The first result that can be inferred from this study is that rotational piezomagnetic anomalies are completely localized at the fault tips. So for detection of this anomaly the magnetic instruments should be installed at these locations. The other important element which has been investigated was the amount of slip along the fault, which shows anomaly intensification by increase in the amount of slip.

1 Introduction

The Mosha Fault, which was first identified by Dellenbach (1964), is the most prominent structure in the southern part of the Central Alborz (Fig. 1). It is an extensive active fault along which Precambrian, Paleozoic and Mesozoic rocks in the north are thrust over Eocene rocks in the frontal Alborz folds to the south (Berberian et al., 1993). The structural geometry of the fault, together with its high angle of dip, indicates that it is a basement involved thrust (e.g. Mitra and Mount, 1998).

The Mosha fault, has experienced several earthquakes of magnitude greater than 6.5 in the years 958, 1665 and 1830 (Berberian and Yeats, 2001). During the XIX century, no strong events were located near Tehran, but several of magnitude greater than 5 was associated with the Mosha fault (Fig. 1).

The magnetization of titanomagnetite-bearing rocks varies under the mechanical stress and consequent time-dependent local magnetic changes. This phenomenon which is known as piezomagnetic field has been inspired by many investigations in earthquake prediction studies and has been reported in the literature (Johnston and Muller, 1987; Sasai and Ishikawa, 1991; Johnston et al., 1994). Several theories proposed for relating piezomagnetic changes with magnetic signals accompanying earthquakes in the vicinity of a fault. Among all efforts, Sasai (1980) successfully developed what is called Green function method for calculating the piezomagnetic effects due to dislocations. Later, based on his theory, Utsugi et al. (2000), derived an analytical solution for the elementary piezomagnetic potentials due to an inclined rectangular fault within a semi-infinite elastic medium.
Fig. 1. Main major faults at the study area. Locations of historical earthquake of the Mosha Fault are also shown.

<table>
<thead>
<tr>
<th>Average Magnetization (J) (A/m)</th>
<th>The main Field at the fault location (nT)</th>
<th>Magnetic Inclination (degree)</th>
<th>Magnetic Declination (degree)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>47850</td>
<td>54.051</td>
<td>4.05</td>
</tr>
</tbody>
</table>

Table 1. The magnetic parameters used for calculation of the rotational piezomagnetic changes for the Mosha fault.

However, the low amplitude nature of piezomagnetic total field changes are imposing serious constrains on our ability for effectively detect this important signals. Mostly they are below the noise level of the measurements. Therefore it seems necessary to use other methods such as measuring rotational piezomagnetic changes in conjunction with total field studies to provide a new insight to the issue.

For this purpose in this study the Piezomagnetic components in the Cartesian coordinate and consequently the rotational piezomagnetic changes for the Mosha fault has been computed. Hence, model calculations have been conducted in order to forecast the rotational piezomagnetic amplitudes in the case of the occurrence of an arbitrary earthquake along the fault.

This information along with the recently acquired magnetic data in the Mosha fault region (Mokhtari et al., 2008) will be used in installing the future magnetic data acquisition system. The system will be part of other sets of instrumentation for earthquake prediction/precursory study in the central Alborz, north of Tehran. In this paper after a brief introduction of the methodology, through numerical modeling of piezomagnetic component for the Mosha fault will be discussed.

2 Methodology

The elementary Piezomagnetic potentials and Piezomagnetic changes in components of the ambient magnetic field have been used in order to find the corresponding relations for the increments in initial declination and inclination at the time of earthquake occurrence.

Let \( W^m \) be the scalar magnetic potential arising from the effect of stress on \( J_m \) which is a component of initial magnetization \( J \). Therefore, \( W^m \) can be expressed as (Sasai, 1991):

\[
W^m(r) = \int \int \Delta u_k(\xi) \omega_{kij}^m(\xi, r) \nu_l(\xi) d\Sigma(\xi)
\]  

In which, \( \Delta u \) denotes a dislocation vector, and \( \omega_{kij}^m \) expresses the elementary Piezomagnetic potential produced by the \( m^{th} \) component of initial magnetization of the crustal rock at the fault zone. \( \nu_l \) stands for a unit vector normal to the surface element \( d\Sigma \) of the fault. Also \( r \) represents the location of observation point and \( \xi \) denotes the location of the point dislocation source.

Considering \( W \) as a scalar potential for the piezomagnetic field of an inclined strike slip fault which has located above the isothermal Curie, a computer program using MATLAB (The MathWorks, Inc.) have been developed. Using this program the Piezomagnetic components in the Cartesian coordinate and consequently the rotational piezomagnetic changes for the above mentioned fault type can be computed. Hence, a model calculation could be carried out in order to forecast the rotational Piezomagnetic amplitudes in the case of the occurrence of an arbitrary earthquake along the fault. The above mentioned methodology has been applied to Mosha fault, which are described in the following section.
Table 2. The fault parameters used for calculation of the rotational piezomagnetic changes for the Mosha fault.

<table>
<thead>
<tr>
<th>Fault Length (2L) (Km)</th>
<th>Fault Width (W) (Km)</th>
<th>Rigidity (µ) (cgs)</th>
<th>Poisson’s Ratio (ν)</th>
<th>Curie Stress (H) (Km)</th>
<th>Stress Sensibility (β) (bar⁻¹)</th>
<th>Dip Sensibility (degree)</th>
<th>Fault Strike</th>
<th>Depth (Km)</th>
</tr>
</thead>
<tbody>
<tr>
<td>70</td>
<td>1</td>
<td>3.5×10¹¹</td>
<td>0.25</td>
<td>15</td>
<td>1.0×10⁻⁴</td>
<td>75</td>
<td>E-W</td>
<td>12</td>
</tr>
</tbody>
</table>

Fig. 2. Declinational Piezomagnetic changes in the case of an amount of 1 m slip along the Mosha fault (MF), in which the ambient fields are (a) 47 850 nT (b) 10 000 nT and (c) 1000 nT.

Fig. 3. Declinational Piezomagnetic changes in the case of an amount of 5 m slip along the Mosha fault (MF), in which the ambient fields are (a) 47 850 nT (b) 10 000 nT and (c) 1000 nT.
Fig. 4. Declinational Piezomagnetic changes in the case of an amount of 10 m slip along the Mosha fault (MF), in which the ambient fields are (a) 47 850 nT (b) 10 000 nT and (c) 1000 nT.

3 Numerical examples

The Mosha fault as a case study has been selected based on its character as being a major active fault to examine the rotational piezomagnetic changes (both Declination and Inclination). In this regards the order of the rotational piezomagnetic changes for earthquakes with specific magnitudes (due to different amount of slip) have been evaluated at the presence of three different main geomagnetic fields (Table 1). The magnetic parameters are taken from the recent magnetic survey conducted in the Mosha fault region (Mokhtari et al., 2008). The other main parameters of the fault are based on Ashkari et al. (2005), Moinabadi and Yassaghi (2007), Ritz et al. (2006) and Guest et al. (2006) given in Table 2.

Using the computer program developed during this study, both declination and inclination changes along the Mosha fault have been examined. Among all the cases being considered, declinational changes showed more significant anomalous behavior compared to inclinational variations which were nearly zero. Therefore, in the following only declinational changes have been illustrated in all figures and are being discussed.

Figures 2–4 show the declinational piezomagnetic changes in the case of 1, 5 and 10 m slip along the fault, in which the ambient fields are (a) actual value of 47 850 nT (b) assumed value of 10 000 nT and (c) assumed value of 1000 nT respectively. The assumed values could be modified and the developed computer program has the capacity of handling any values. The above values are only to illustrate the trend or behavior of the piezomagnetic changes under different situations.

The first result that can be inferred from the figures is that the rotational piezomagnetic changes are completely localized at the fault tips. So we may loose these significant data if the instruments being installed even a small distance from these locations. Mokhtari et al. (2007) and Groshkov et al. (2007) using Morphostructural Zoning Method have discussed the most likely occurrence of earthquake events in the Alborz region and showed that these are being associated with intersection of faults which is in agreement with the above mentioned results.

The other important element that affects the piezomagnetic changes is the amount of slip (magnitudes) along the fault. As shown in Figs. 2–4 by an increase in the amount of slip the changes would become more intensified.

In addition the influence of a specific magnetic field at the fault tips has been examined. A careful study of all numerical examples reveals that by decrease in the value of magnetic field from the real amount; cases (a) to assumed value 1000 nT; cases (c), the amplitude of changes show a significant increase in the amplitude of the anomalies (Figs. 2–4).

4 Conclusions

In this study a computer program under MATLAB (The MathWorks, Inc.) has been developed for computation of the rotational piezomagnetic changes for the Mosha fault. Based on the result it has been concluded that among the parameters examined the amount of slip and the value of total magnetic field has major contribution. In addition due to concentration of changes at the tips of fault, for future observation of the
piezomagnetic changes for earthquake prediction/precursor purposes it is important to install the magnetometers very close to these locations.

The above mentioned result will be further examined along with other earthquake precursory methods in Central Alborz, north of Tehran.

Edited by: P. F. Biagi
Reviewed by: two anonymous referees

References

Dellenbach, J.: Contribution à l’étude géologique de la région située l’est de Te’he’ran (Iran), Faculty of Science, University of Strasbourg (France), 117 pp., 1964.