Rainfall observation from X-band, space-borne, synthetic aperture radar

J. A. Weinman1, F. S. Marzano2, W. J. Plant3, A. Mugnai4, and N. Pierdicca2

1Atmospheric Sciences Dept., University of Washington, Seattle, WA, 98195 USA  
2Electrical Engineering Dept., University of Rome, “La Sapienza”, 00184 Roma, Italy  
3Applied Physics Laboratory, University of Washington, Seattle, WA, 98195 USA  
4Atmospheric Physics Institute, National Research Council of Italy, 00044 Frascati, Italy

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Abstract. Satellites carrying X-band Synthetic Aperture Radars (SAR) have recently been launched by several countries. These provide new opportunities to measure precipitation with higher spatial resolution than has heretofore been possible. Two algorithms to retrieve precipitation from such measurements over land have been developed, and the retrieved rainfall distributions were found to be consistent. A maritime rainfall distribution obtained from dual frequency (X and C-band) data was used to compute the Differential Polarized Phase Shift. The computed Differential Polarized Phase Shift compared well with the value measured from space. Finally, we show a comparison between a recent X-band SAR image of a precipitation distribution and an observation of the same rainfall from ground-based operational weather radar. Although no quantitative comparison of retrieved and conventional rainfall distributions could be made with the available data at this time, the results presented here point the way to such comparisons.

1 Introduction

Global precipitation measurements are needed by weather forecasters and climate modelers because the release of latent heating has a profound effect on the performance of such models. With the improvement in computer capability, forecast models will be able to operate with more realistic physics, and with higher spatial and temporal resolution, Randall (2006). The Japanese Earth Simulator is already being run globally with ~10 km horizontal resolution, Ohfuchi et al. (2007). Several mesoscale models are now running operationally with less than 4 km horizontal resolution, and Chen et al. (2007) showed that mesoscale models with 1.67 km resolution were needed to resolve the inner core structure of hurricanes.

Since the 1980s much of our understanding of global oceanic precipitation has come from space-borne passive microwave radiometers. Space-borne microwave radiometers have spatial resolution in excess of 10 km. Detailed observations of hurricanes over oceans are obscured by that limitation.

Microwave radiometric measurements of rainfall over land rely on the scattering properties of ice in the upper regions of precipitating clouds. However Bennartz and Petty (2001) showed that the relationship between surface rainfall rates and the scattering properties of frozen hydrometeors is problematic.

These limitations can be mitigated by space-borne radars. The Precipitation Radar (PR) aboard the Tropical Rainfall Measurement Mission (TRMM) satellite has provided unique precipitation measurements as demonstrated by Kummerow et al. (2000), but even the 4 km horizontal resolution, and the Signal/Noise Ratio (SNR) floor of the PR may inhibit the measurement of compact rain cells, Durden et al. (1998).

C-band and L-band (~5 and ~21 cm wavelengths, respectively) Synthetic Aperture Radars (SARs) have a long heritage of Earth observation with high spatial resolution. However such radars are insensitive to rainfall in the atmosphere. Atlas and Moore (1987), Jameson et al. (1997), Moore et al. (1997) Melsheimer et al. (1998) and Alpers and Melsheimer (2004) showed that SARs operating at the shorter wavelength X-band (~3 cm wavelength) could detect rainfall. With ~100 m resolution, X-band Synthetic Aperture Radars (X-SARs) can provide new insights into the structure of precipitating clouds.

In order to illustrate how rainfall may be retrieved from X-SAR measurements, we used data from the STS-59 and STS-68 Shuttle missions of 1994 that carried the first X-SAR
Fig. 1. Left: View around Noakhali, Bangladesh (22.8° N x 91.2° E) on 7 October 1994 with no rain present. Right: Same scene on 18 April 1994. Note scattering by frozen hydrometeors in the upper right, scattering and attenuation by rain in middle-lower right, and absorption mainly by rain with little ice in the lower left. The maximum NRCS of the scattered signal is \(\sim -3\) dB and the minimum NRCS value in the shaded area is \(\sim -30\) dB.

Fig. 2. Upper: Schematic view of the model used to compute the NRCS from a horizontally variable two layer precipitating cloud. Lower: Schematic NRCS (dB) as a function of cross-track scanning distance (km) showing enhanced values on the left of the cross-over point caused by scattering from the cloud top and attenuation from rain in the lower cloud on the right. The background NRCS is \(\sigma^0\).

The years following 2007 have provided new opportunities to measure rainfall distributions from X-SARs. Three of four CosmoSkyMed satellites have already been launched, and the last one will be launched in 2009, Caltagirone et al. (2007). The TerraSAR-X was also launched in 2007, Buckreuss et al. (2003), and TecSAR was successfully launched in January 2008, Sharay and Naftaly (2006). A dual frequency, X and Ku-band SAR has been approved for development by ESA, Rott et al. (2007). Table 1 summarizes some features of the X-SAR systems that will operate during the coming decade.

2 The normalized radar cross section model

Figure 2 shows a schematic view of a cloud scanned from the left by an X-SAR. The surface cross section is \(\sigma^0\). The vertical direction is \(z\), and the cross track scan direction is \(\chi\), whose origin may be set at a distance \(z_f / \tan \theta\) to the left of the precipitation, where \(z_f\) designates the top of the cloud. The propagation vectors are depicted as solid lines. The propagation direction is oriented at an angle, \(\theta\), from nadir. The scattering volume is bounded by the dashed lines that are orthogonal to the propagation direction.

As the X-SAR scans from left to right, the Normalized Radar Cross Section (NRCS) first increases above the background value due to scattering by the frozen hydrometeors in the upper part of the cloud. As the X-SAR continues to scan further to the right, the signal from the underlying surface is reduced by attenuation of radiation due to the rain. The NRCS increases again as the scanned footprint moves to the right beyond the precipitating cloud, and less rain is intercepted.
Table 1. Characteristics of previous, existing, and planned X-band SARs.

<table>
<thead>
<tr>
<th>Mission</th>
<th>Polarization capability</th>
<th>ScanSAR swath width (km)</th>
<th>ScanSAR resolution (m)</th>
<th>Orbit altitude (km)</th>
<th>Incidence angle range (°)</th>
<th>Mission duration</th>
</tr>
</thead>
<tbody>
<tr>
<td>Shuttle STS-59.68</td>
<td>V, V</td>
<td>15–60</td>
<td>20×30</td>
<td>225</td>
<td>20–55</td>
<td>2×10 days 1994</td>
</tr>
<tr>
<td>Cosmo Sky-Med (4 satellites)</td>
<td>HH, VV selectable</td>
<td>200</td>
<td>30–100</td>
<td>620</td>
<td>25–57</td>
<td>5 yrs 9 Jan 2007</td>
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<tr>
<td>TerraSAR-X</td>
<td>HH, HV</td>
<td>100</td>
<td>16</td>
<td>514</td>
<td>20–45</td>
<td>5 yrs 15 Jan 2008</td>
</tr>
<tr>
<td></td>
<td>VH, VV</td>
<td></td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>TecSAR</td>
<td>HH, HV</td>
<td>100</td>
<td>20</td>
<td>550</td>
<td>4–8 yrs</td>
<td>4–8 yrs 21 Jan 2008</td>
</tr>
<tr>
<td></td>
<td>VH, VV</td>
<td></td>
<td></td>
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<tr>
<td>Kompasat-5</td>
<td>HH, HV</td>
<td>100</td>
<td>20</td>
<td>685</td>
<td>5 yrs</td>
<td>5 yrs 2009 start</td>
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<tr>
<td></td>
<td>VH, VV</td>
<td></td>
<td></td>
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<td></td>
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<tr>
<td>CoRe-H2O</td>
<td>VH, VV</td>
<td>100</td>
<td>25×9</td>
<td>30–40</td>
<td>5 yrs</td>
<td>5 yrs TBD</td>
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<td>Dual Frequency</td>
<td></td>
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<td>With 17.2 GHz</td>
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The NRCS, $\sigma_{SAR}$, consists of two parts: namely scattering from the surface, $\sigma_{srf}$, and scattering by the precipitation, $\sigma_{vol}$, such that:

$$\sigma_{SAR} = \sigma_{srf} + \sigma_{vol}$$

where

$$\sigma_{srf}(x) = \sigma^0(x)e^{-2\int_{x-x''}^{x-x'''} k(x') \frac{dx'}{\cos \theta}}$$

$$\sigma_{vol}(x) = \sin \theta \int_{x}^{x'} \eta(x') e^{-2\int_{x-x''}^{x-x'''} k(x') \frac{dx'}{\cos \theta}}$$

The projection of the propagation vector onto the cross track direction is designated $x''$, and the projection along the cross track direction of the vector defining the scattering volume is $x'$. It follows that

$$x' - x'' = (z'' - z') \tan \theta$$

$$z' = (x' - x) \tan \theta.$$

and

$$X(x, \theta) = x' + (x' - x) \tan^2 \theta - z_t \tan \theta.$$

Attenuation takes place along the propagation path with a coefficient represented by, $k=aR^b$ (km$^{-1}$). The volumetric scattering occurs within a slice of oblique thickness $\Delta r$ in the direction perpendicular to the propagation path from the radar. The reflectivity within the volume element, $\eta$ (km$^{-1}$), in terms of wavelength, $\lambda$ (cm), is

$$\eta = 10^{-5} \frac{\pi^5 |K|^2}{\lambda^4} Z_e$$

and the attenuation corrected effective radar reflectivity factor is $Z_e = cR^d$.

Numerous types of hydrometeors, characterized by the rainfall rate, $R$ (mm/h), may occur within precipitating clouds, and they contribute differently to $\eta$ and $k$. Thus $a$, $b$, $c$, and $d$ are constants that depend on the phase, density, and size distribution of the hydrometeors. They can initially be given a priori values, as is done for computations of conventional single frequency radar returns.

### 3 Model precipitation distributions

The model rainfall rate distributions, $R(x, z)$, were represented in the form,

$$R(x, z) = H(x)V(z)$$

as in Marzano et al. (2006), Weinman and Marzano (2008), and by Marzano and Weinman (2008).

The vertical distributions

$$V(z) = \frac{V(z_0)(z_t-z)/(z_t-z_0)}{V(0)(0.85+0.15[(z_0-z)/z_0]^{0.5})}$$

for $z_0 \leq z \leq z_t$

$$V(0) = 0.85$$

were representations extracted from Contoured Frequency by Altitude Diagrams (CFAD) found by Yuter and Houze (1995). The snow cloud top heights were $z_t$. The freezing level heights, $z_0$, could be determined from surface temperatures by assuming that the lapse rate was 5.8 C/km or from temperature profiles obtained from nearby radiosonde ascents.
The horizontal distributions, $H(x)$, were the most variable, and they were derived from two distinct algorithms.

4 Precipitation retrieval algorithms over homogeneous land

Two separate retrieval algorithms were developed to infer $R(x, z)$. One was statistical and the other was an analytical solution to the Volterra Integral Equation (VIE) of the second kind.

Briefly summarized, the statistical algorithm described in Marzano and Weinman (2008) and Weinman and Marzano (2008) finds a crossing node, $x_o$, where the NRCS makes a transition from enhancement due to scattering to reduction due to attenuation. The algorithm then relates moments of the $H(x)$ to moments of the NRCS about $x_o$. It also determines NRCS gradients at several locations. Eleven parameters thus comprise components of a vector, $x_{SAR}$. The shape of $H(x)$ is obtained by minimizing the quantity

$$d(c_H) = (x_{SAR} - m_{SAR})^T C_{CSAR}^{-1} (x_{SAR} - m_{SAR})$$

where the subscript $C$ identifies the cloud shape class, and $m$ is the vector of the mean parameters. The asterisk represents the transpose of a vector, and $C_{CSAR}$ is the covariance matrix of the population of model clouds.

The VIE retrieval algorithm was first described in Pichugin and Spiridonov (1991). The NRCS equation presented at the beginning of this paper was transformed, by a series of algebraic manipulations, to a form:

$$P(x) = f(x) + \lambda \int_{x^*}^{x} K(x, t)P(t)dt$$

where $P(\ldots)$ is the transformed function of $H(x)$, and $K(x, t)$, $f(x)$ and $\lambda$ are transformations of clusters of various parameters that appear in the NRCS formulation. The reader is referred to Pichugin and Spiridonov (1991) and to Marzano and Weinman (2008) for a comprehensive description of this method.

An X-band image of a convective cell in the Amazon is shown in Fig. 3 (left) along with the retrieved $R(x, z)$ distributions (center and right) obtained from the statistical and VIE retrieval algorithms respectively. Although no independent validation was available, the agreement between the two results is reasonably consistent.

5 Dual frequency precipitation retrieval over an inhomogeneous sea surface

The determination of rainfall over a sea surface is more difficult than over land because sea surface NRCS values are highly variable, and that variability is related to the rainfall rate. The wind field that roughens the sea surface around precipitating clouds, and the impinging raindrops that damp surface waves complicate the sea surface structure. Examples of sea surface roughness patterns around precipitation observed by C-band SARs (C-SARs) are shown in Alpers and Melsheimer (2004).

Although the retrieval of marine rainfall from single frequency X-SAR radar cross sections is hobbled by this surface cross section ambiguity, the problem becomes tractable when C and X-band SARs observe the same scene. The model of Contreras and Plant (2006) was used to compute the relationship between C and X-band values of $\sigma^0(x)$ for wind-roughened, and rain impacted sea surfaces. Those model computations were run for VV and HH polarization, and for incidence angles of 30, 45 and 60 degrees. Various combinations of rainfall rates, 0, 5, 10, and 40 mm/h along with wind speeds values of 3, 4, 5, 10, 15, and 20 m/s at 10 m above the

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**Fig. 3.** Left: X-SAR image of an isolated convective cell over Amazonas, Brazil (9.01° S × 68.38° W) obtained at 18:45 UTC on 15 April 1994. The X-SAR viewed this scene from the left and the satellite passed from the top of the scene to the bottom. Center: The rainfall rate distribution, $R(x, z)$, along the transect $A-A'$ retrieved by the statistical algorithm, and right: that retrieved by the VIE solution.
Fig. 4. Comparison between model $\sigma^v_C$ and $\sigma^v_X$ at VV and HH polarization for wind roughened and rain impacted sea surfaces. Black (o), red (*) and blue () represent up-wind, cross-wind and down-wind computations respectively. The left and right columns present the relations among the VV and HH polarized $\sigma^v$ respectively. The cross section model of Contreras and Plant (2006) was used to model various combinations of $R=0, 5, 10,$ and $40$ mm/h and $V_{10}=3, 4, 5, 10, 15,$ and $20$ m/s, Values for $V_{10}=25, 30, 35, 45$ m/s for wind roughened surfaces were interpolated from measured values by Fernandez et al. (2006).

sea surface were considered. The viewing directions could be up-wind, cross-wind and down-wind. In addition, sea surface cross section measurements for wind-roughened sea surfaces found by Fernandez et al. (2006) were interpolated to yield comparable relationships for $25, 30, 35, 45$ m/s, with no rain. These results are shown in Fig. 4. Linear fits to those cross sections, including the wind roughened sea surface measurements by Fernandez et al. (2006) can be fitted by:
Fig. 5. Upper left: An X-band image observed over the Gulf of Mexico, 17 April 1994 at 18:47 UTC during STS-59, first presented in Melsheimer et al. (1998) as part of their Fig. 3. Upper right: The X-band NRCS scan along the red transect $A-A'$ in Fig. 7a of the Melsheimer et al. (1998) paper (- - - -). The NRCS computed from the model $R(x, z)$ distribution found in our study was (-----). The $\sigma^0(x)$ was obtained from the transformed C-band NRCS. Lower left: The model C-band DPPS for the same $R(x, z)$ compared to that presented in Fig. 7d of Melsheimer et al. (1998) (- - - -). The $K_{dP} - R$ relationship was an extrapolation from Teschl et al. (2006) and private communication. Lower right: The $R(x, z)$ distribution used in the model. Note that the width of this cell is $\sim 3$ km. This cell width is consistent with the along-track dimension shown in the upper left. This cell would just fill one TRMM PR footprint.

$$\sigma_{C}^{0X} = f_{X-C}\sigma_{C}^{0C}$$

It is noteworthy that the model data from wind roughened surfaces only, and those from sea surfaces subjected to wind roughening and rain impact damping follow common linear trends within $\sim 15\%$. Values for $f_{X-C}$ for VV polarization at 30°, 45°, and 60° are 1.53, 1.47 and 1.16, respectively, and those for HH polarization are 1.50, 1.88 and 1.42.

A sample of data presented in Fig. 7 of Melsheimer et al. (1998) was analyzed to demonstrate the use of dual frequency data. It was noted from various model runs that rainfall had a minor effect on C-band NRCS measurements ($\sim 0.3$ dB) so that $\sigma_{C}^{0C}(x) \approx \sigma_{SAR}^{0C}(x)$. The background $\sigma_{C}^{0X}(x)$ was thus derived from the application of the linear equation shown above to yield $\sigma_{C}^{0C}(x)$ presented in Fig. 7a of Melsheimer et al. (1998). The X-band NRCS measured along $A-A'$, and that computed from a model with transformed sea surface NRCS values is shown in Fig. 5 (upper right). The $R(x, z)$ that produces this NRCS scan is shown in Fig. 5 (lower right).

6 The C-band differential polarized phase shift as a form of validation

Bringi and Chandrasekhar (2001) showed that the Differential Polarized Phase Shift (DPPS) provides a measure of rainfall rate along a propagation path. Although no measurements of the X-band DPPS were available, the C-band DPPS, shown in Fig. 5 (lower left), provides a check on the validity of the rainfall rate distribution, $R(x, z)$, derived from the X-band NRCS.
The DPPS is determined by the integral of the specific differential phase, $K_{dp}$, along the two way propagation path, i.e.

$$\text{DPPS} = \frac{2}{\sigma_{\text{SAR}} \cos \theta} \left\{ \int_0^{z_0} K_{dp}[x(z)] \sigma_{\text{srf}}[x(z)] \, dz + \int_0^{z_0} K_{dp}[x(z)] \sigma_{\text{vol}}[x(z)] \, dz \right\}$$

where $z_0$ is the height of the freezing layer. We used the C-band $K_{dp} - R$ values for raindrops tabulated by Teschl et al. (2006). These were generalized to account for incidence angles, $\theta$, down to 30° to yield:

$$K_{dp} = \frac{0.168}{\lambda} \sin^2 \theta R^{1.20} \left( ^\circ / \text{km} \right)$$

Ryzhkov and Zrnic (1998) found that $K_{dp}$, for snow was $\sim 0.03 ^\circ / \text{km}$ at S-band ($\sim 10 \text{ cm wavelength}$). That value was nearly independent of the melted rainfall rate. The $K_{dp}$, of snow is expected to be about twice that large at C-band. Marzano and Weinman (2008) computed $K_{dp}$, for snow at C-band and those computations also yield small values. Because of the irregular shape of snow, there was even some uncertainty about the sign of $K_{dp}$. In view of these considerations, we neglected the effect of snow on the C-band DPPS.

### 7 Comparison of rainfall distributions observed from ground based radar and X-SAR

This discussion has been based on data available from the 1994 Shuttle missions. However new opportunities to measure X-band NRCS are rapidly becoming available. Figure 6 (upper) displays a TerraSAR-X image of the region around Orleans, France obtained on 16 March 2008 in which the presence of rain is identified within the red ellipse. The Plan Position Indicator (PPI) display recorded at a height of 2 km by the Trappes operational radar (lower) confirms the presence of rain in the scene. (The Loire River provides a reference in both images.) A 12:00 UTC sounding from Trappes, France suggested that the freezing level was at 1.6 km so that the PPI probably responded to scattering by frozen hydrometeors. Digital data files for this case were not available as this document was being written, so a quantitative evaluation of the rainfall retrieval could not be conducted.

### 8 Preliminary conclusion and discussion

This study employed rainfall retrieval algorithms based on statistical and analytical VIE methods to infer the rainfall distribution over the uniform land surface of the Amazon Basin. Although the techniques are quite distinct, they gave distributions that were in reasonable agreement. It should however be stressed that we had no independent verification of the validity of those retrieved distributions.

In spite of the variability of the NRCS of sea surfaces in the proximity of rainfall, we were able to take advantage of the insensitivity of the C-band NRCS to atmospheric rain to infer the C-band NRCS of the surface. That C-band NRCS could be transformed to X-band sea surface NRCSs that were needed as boundary conditions to compute the X-band NRCS.

A combined C and X-band retrieval from two SARs carried on satellites in a common polar orbital plane may yield additional information regarding precipitation distributions. One such pair of SARs might be the TerraSAR-X and the RadarSAT-2.

Although we had no independent rainfall measurements with which to validate our retrieved maritime rainfall rate distribution, we had measurements of the C-band DPPS. The measured and modeled DPPS were reasonably consistent. However several simplifying assumptions about the $K_{dp}$, of the various species of hydrometeors were made. More comprehensive polarization measurements would lend additional
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